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## Introduction

In many problems chance (or probability) plays an important role. Decision analysis is the general name that is given to techniques for analyzing problems containing risk/uncertainty/probabilities. E.g., decision trees are a specific tool of decision analysis. For the following example draw the decision tree and solve it:

## Example MDG

The Metal Discovery Group (MDG) is a company set up to conduct geological explorations of parcels of land in order to ascertain whether significant metal deposits (worthy of further commercial exploitation) are present or not. Current MDG has an option to purchase outright a parcel of land for $£ 4 \mathrm{~m}$.

If MDG purchases this parcel of land then it will conduct a geological exploration of the land. Past experience indicates that for the type of parcel of land under consideration geological explorations cost approximately $£ 2 \mathrm{~m}$ and yield significant metal deposits as follows:

- gold $1.01 \%$ chance
- silver $0.6 \%$ chance

Only one of these two metals is ever found (if at all), i.e. there is no chance of finding two or more of these metals and no chance of finding any other metal.

If gold is found then the parcel of land can be sold for $£ 320 \mathrm{~m}$ and if silver is found the parcel of land can be sold for $£ 160 \mathrm{~m}$.

MDG can, if they wish, pay $£ 250 \mathrm{k}$ for the right to conduct a three-day test exploration before deciding whether to purchase the parcel of land or not. Such three-day test explorations can only give a preliminary indication of whether significant metal deposits are present or not and past experience indicates that three-day test explorations cost $£ 250 \mathrm{k}$ and indicate that significant metal deposits are unlikely being present $50 \%$ of the time.

If the three-day test explorations indicate significant metal deposits then the chances of finding gold and silver increase to $2 \%$ and $1 \%$ respectively. If the three-day test explorations indicate that significant metal deposits are unlikely then the chances of finding gold and silver is not zero but it decreases to $0.02 \%$ and $0.2 \%$ respectively.

