

6. Tutorium - Resultate

06.05.2016

6.1 Elektrische Feldenergie

$$a) \rho(\vec{r}) = \sigma_0 \delta(r - R), \text{ mit } \sigma_0 = \frac{Q}{4\pi R^2}.$$

$$V(\vec{r}) = \frac{Q}{4\pi\epsilon_0} \begin{cases} \frac{1}{r} & r > R \\ \frac{1}{R} & r < R \end{cases}$$

$$\vec{E}(\vec{r}) = \vec{e}_r \frac{Q}{4\pi\epsilon_0} \begin{cases} \frac{1}{r^2} & r > R \\ 0 & r < R \end{cases}$$

$$b) \vec{E}_r(r \rightarrow R^+) - \vec{E}_r(r \rightarrow R^-) = \frac{Q}{4\pi\epsilon_0 R^2} = \frac{\sigma_0}{\epsilon_0}$$

$$c) U = \frac{1}{2} \frac{Q^2}{4\pi\epsilon_0} \frac{1}{R}$$

6.2 Multipolmomente eines Kreuzes

$$a) \rho(\vec{x}) = \lambda [\theta(a+x)\theta(a-x)\delta(y)\delta(z) + \theta(b+y)\theta(b-y)\delta(x)\delta(z)]$$

$$Q = 2\lambda(a+b)$$

$$b) p_i = 0$$

$$Q_{xx} = \frac{2\lambda}{9}(2a^3 - b^3)$$

$$Q_{yy} = \frac{2\lambda}{9}(-a^3 + 2b^3)$$

$$Q_{zz} = \frac{2\lambda}{9}(-a^3 - b^3)$$

$$Q_{xy} = Q_{yx} = \dots = 0$$

$$c) \phi(0, 0, z) = \frac{2\lambda(a+b)}{z} + \frac{\lambda(-a^3 - b^3)}{3z^3}$$

$$d) \vec{E}(0, 0, z) = \left[\frac{2\lambda(a+b)}{z^2} + \frac{\lambda(-a^3 - b^3)}{z^4} \right] \vec{e}_z$$

6.3 Punktdipol und Punktladung

$$a) \vec{F}_q = -\frac{1}{4\pi\epsilon_0} \frac{qp}{x_1^3} \vec{e}_z$$

$$\vec{F}_d = \frac{1}{4\pi\epsilon_0} \frac{qp}{x_1^3} \vec{e}_z = -\vec{F}_q$$

$$b) 0.$$

$$c) W = \frac{1}{4\pi\epsilon_0} \frac{qpz_2}{(x_2^2 + y_2^2 + z_2^2)^{3/2}}$$

$$\vec{F} = \frac{qp}{4\pi\epsilon_0} \left(\frac{3z_2 \vec{x}_2}{r_2^3} - \frac{\vec{e}_z}{r_2^3} \right)$$