Important: Answers must be a hard copy and submitted to the office in CA0421 by December 17, 2014 at 4 pm . The work must be original.

Fig. 1 shows a lumped mass model of a positioning system using a piezo actuator. The power is provided by a voltage amplifier. The disturbance to be corrected has a power spectral density of $1 \mathrm{~nm} / \sqrt{\mathrm{Hz}}$ and a bandwidth of 7.5 kHz . The assignment is to compute amplifier requirements in terms of voltage and current.


Fig. 1: A lumped mass model of a positioning system and the stacked piezo actuator

| Parameter | Value | Unit |  |
| :---: | :---: | :---: | :---: |
| $Y$ | $53 \cdot 10^{9}$ | $\mathrm{~N} / \mathrm{m}^{2}$ | Youngs modulus |
| $m$ | 10 | g | Weight mass |
| $\rho$ | $7.85 \cdot 10^{3}$ | $\mathrm{Kg} / \mathrm{m}^{3}$ | Density piezo |
| $c$ | 10 | $\mathrm{~N} /(\mathrm{m} / \mathrm{s})$ | Damping |
| $I_{0}$ | 25 | mm | Length piezo |
| $r$ | 5 | mm | Radius piezo |
| $d$ | $195 \cdot 10^{-12}$ | $\mathrm{~m} / \mathrm{V}$ | Piezoelectric <br> coefficient |
| $\varepsilon$ | $1.68 \cdot 10^{-8}$ | $\mathrm{~F} / \mathrm{m}$ | Dielectric coefficient |
| $n$ | 170 | $\sim$ | Number of stacks |
| $R$ | 50 | $\Omega$ | Output impedance |

i. Determine the mass, stiffness and the capacity of the piezo [15\%]
ii. Determine the transfer function from input voltage to displacement and the impedance of the piezo amplifier [30\%]
iii. Determine the required voltage and current [30\%]

