

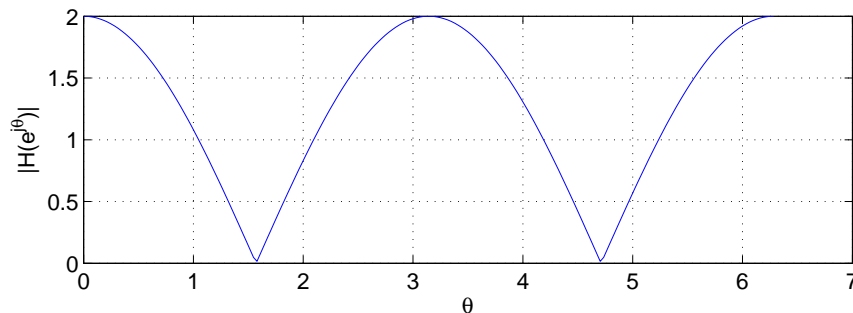
1. Beispiel:

Gruppe A

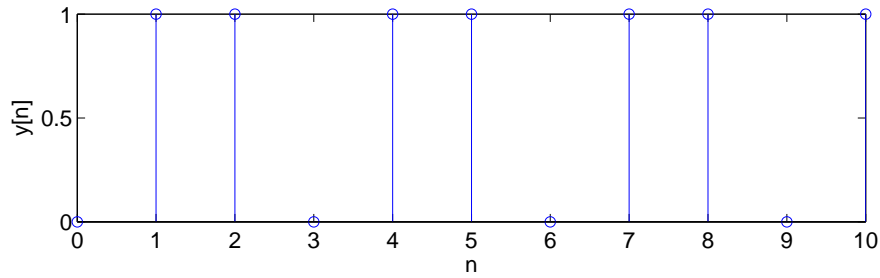
- a) $h[n] = \delta[n] + \frac{1}{2} \delta[n - 1]$, Skizze trivial.
- b) $a[n] = \sum_{k=-\infty}^n h[k] = \sigma[n] + \frac{1}{2} \sigma[n - 1]$, Skizze trivial.
- c) $y[n] = x[n] + \frac{1}{2} x[n - 1] = \dots = \frac{1}{2} \left(1 + \sum_{k=-\infty}^{\infty} \delta[n + 2k] \right)$.
- d) $N_x = 2, c_k = \frac{1}{2} \sum_{n=0}^1 \delta[n] e^{-j\pi kn} = \frac{1}{2}, \quad k = 0, 1.$
- e) $N_y = 2, d_k = \frac{1}{2} \sum_{n=0}^1 \left(\delta[n] + \frac{1}{2} \delta[n - 1] \right) e^{-j\pi kn} = \begin{cases} \frac{3}{4} & k = 0 \\ \frac{1}{4} & k = 1 \end{cases}$
 oder direkt aus c): $d_k = \frac{1}{2} (\delta[k] + c_k).$

Gruppe B

- a) $H(e^{j\theta}) = e^{-j\theta} + e^{j\theta} = 2 \cos \theta$



- b) $a[n] = \sum_{k=-\infty}^n h[k] = \sigma[n - 1] + \sigma[n + 1]$, Skizze trivial.
- c) $x[n] = \sum_{k=-\infty}^{\infty} \delta[n + 3k]$
 $y[n] = x[n - 1] + x[n + 1] = \dots = 1 - \sum_{k=-\infty}^{\infty} \delta[n + 3k]$



d) $N_x = 3, c_k = \frac{1}{3} \sum_{n=0}^2 \delta[n] e^{-j \frac{2\pi}{3} kn} = \frac{1}{3}, \quad k = 0, 1, 2.$

e) $N_y = 3$, aus $y[n] = 1 - x[n]$ folgt wegen Linearität $d_k = \delta[k] - c_k = \begin{cases} \frac{2}{3} & k = 0 \\ -\frac{1}{3} & k = 1, 2 \end{cases}.$

2. Beispiel:

Gruppe A

a) $y[n] = FT^{-1} \{ H(e^{j\theta}) X(e^{j\theta}) \} = 2 \delta[n + 1] + \frac{1}{4} \delta[n - 2]$, Skizze trivial.

Formelsammlung: $e^{\pm j\theta} \iff \delta[n \pm 1]$ und $\frac{1}{1 - \frac{1}{2} e^{-j\theta}} \iff \left(\frac{1}{2}\right)^n \sigma[n]$.

b) $y[n] = (x * h)[n] = 2 \delta[n + 1] + \frac{1}{4} \delta[n - 2]$

mit $h[n] = 2 \delta[n + 1] - \frac{1}{2} \delta[n - 1]$ und $x[n] = \left(\frac{1}{2}\right)^n \sigma[n] - \frac{1}{2} \delta[n - 1]$.

Gruppe B

a) $y[n] = \frac{1}{2} \delta[n - 1] + \frac{1}{4} \delta[n - 2]$, Skizze trivial.

b) $H(e^{j\theta}) = 1 - \frac{1}{4} e^{-j2\theta}, \quad X(e^{j\theta}) = -1 + \frac{1}{1 - \frac{1}{2} e^{-j\theta}},$

$y[n] = FT^{-1} \{ H(e^{j\theta}) X(e^{j\theta}) \} = \frac{1}{2} \delta[n - 1] + \frac{1}{4} \delta[n - 2].$

3. Beispiel:

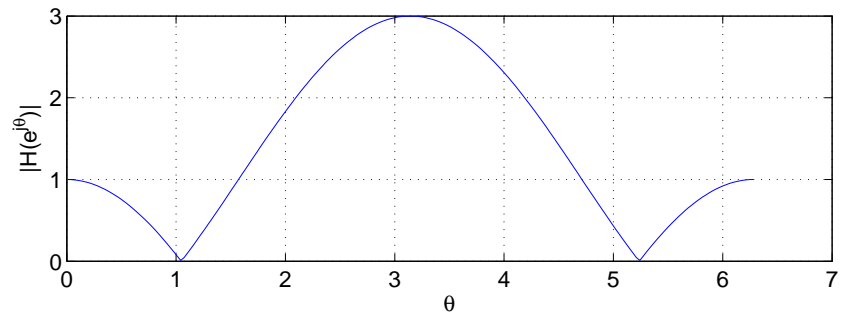
Gruppe A

a) stabil, da Impulsantwort absolut summierbar ist $\sum_{n=-\infty}^{\infty} |h[n]| < \infty.$

b) akausal, da $h[n] \neq 0, n < 0.$

c) $h[n] = -\delta[n - 1] + \delta[n] - \delta[n + 1]$, Skizze trivial.

d) $H(e^{j\theta}) = -e^{-j\theta} + 1 - e^{j\theta} = 1 - 2 \cos \theta.$



Gruppe B

- a) stabil, da Impulsantwort absolut summierbar ist $\sum_{n=-\infty}^{\infty} |h[n]| < \infty$.
- b) akausal, da $h[n] \neq 0, n < 0$.
- c) $h[n] = \frac{1}{2} \delta[n+2] + \delta[n+1] + \frac{1}{2} \delta[n]$, Skizze trivial.
- d) $H(e^{j\theta}) = \frac{1}{2} e^{j2\theta} + e^{j\theta} + \frac{1}{2} = e^{j\theta} (1 + \cos \theta)$.

